

DIGITAL CONTROL SYSTEMS

(Control Systems)

Time: 3 Hours

Max Marks: 60

Answer any FIVE questions. All questions carry EQUAL marks.

1. a. State the advantages and disadvantages of digital data systems?
 b. With a suitable circuit, explain the operation of sampler and hold devices. Also derive the transfer function of zero-order hold. [4M+8M]

2. a. Obtain the z Transform of the following $x(k)$
 $x(k) = 0.1e^{-0.4k} + 0.2e^{-0.2k}$, $k=0,1,2, \dots$. Assume that $x(k)=0$ for $k<0$.

- b. Obtain the inverse z-transform of the following

i. $X(z) = \frac{z^{-1}}{(z-0.5)^2}$ and

ii. $X(z) = \frac{z^{-2}}{(z-0.5)^2}$

[4M+4M+4M]

6. The weighting sequence of a linear discrete-data system is

$$c(k) = \begin{cases} 0.1e^{-0.4k} & k \geq 0 \\ 0 & k < 0 \end{cases} \quad G(z)$$

- (i). Find the transfer function $G(Z)$ of the system.

- (ii) Let the input be $r(k) = u_s(k)$, the unit step sequence. Find the output $c(k)$ in closed form. Find the final value of $C(k)$ as $N \rightarrow \infty$. [EM+7M]

4. Construct the bode diagram of the open loop transfer function

$$G(Z) = \frac{C(z)}{E(z)} \text{ with } Z = e^{j\omega T}, 0 \leq \omega \leq \frac{U_v}{2} \text{ for the system } W_X(Y) = \frac{Y^3}{Y^2 + 1}, T = 0.1 \text{ s.}$$

Determine the gain margin and phase margin of the system.

[12M]

- E. Find the block diagrams of direct programs for the digital controllers given

a. $X(z) = \frac{z^{-1}(z-0.5)}{(z-0.5)^2(z-0.2)}$

b. $X(z) = \frac{z^{-2}(z-0.5)}{(z-0.5)^2}$

c. $X(z) = \frac{z^{-1}(z-0.5)}{(z-0.5)^2}$

[4M+4M+4M]

6. a. Give the properties of state transition matrix.

b. Find the state transition equations of the following systems by means of the state diagram method.

$$-(z + 1) / d(z) + e f(z)$$

The initial states are given as $x(0)$

$$d(z) = z^2 + 0.5z + 0.6, \quad e = 1, \quad f(z) = z^0 \quad [4M+8M]$$

7. Given the discrete data control system

$$-(z + 1) / d(z) + e f(z)$$

$$i(z) / [z - 0.5]$$

Where

$$d(z) = z^2 + 0.4z + 0.46, \quad e = 1, \quad f(z) = [1 \quad 4]z$$

The control is realized through state feedback,

$$f(z) = 4W(z) + 4[C_1 \quad C_2]x(z)$$

Where g_1 and g_2 are real constants. Determine the values of g_1 and g_2 that must be avoided for the system to be completely observable. [12M]

8. a. Discuss about dead beat control?

b. Consider the system given by

$$j(z) = \frac{z^3 - 1}{z^2 - 1} / d(z) + g_1 f(z)$$

Determine the state feedback gain matrix 'k' such that when the control signal is given by $f(z) = 4z - 4$ the closed system exhibits the dead beat response. [4M+8M]