

III B.Tech.(CCC) Supplementary Examinations, June 2009
FINITE ELEMENT METHOD
(Mechanical Engineering)

Time: 3 hours

Max Marks: 100

Answer any FIVE Questions
 All Questions carry equal marks

1. If a displacement field is described as follows,

$$u = (-x^2 + 2y^2 + 6xy)10^{-4} \text{ and } v = (3x + 6y - y^2)10^{-4}$$
 Determine the strain components ϵ_{xx} , ϵ_{yy} , and ϵ_{xy} at the point $x=1$; $y = 0$. [20]
2. With a suitable example explain the formulation of finite element equations by direct approach. Assume suitable data for the example. Use I-D analysis [20]
3. For the truss structure shown in figure 3 is subjected to a horizontal load of 4 kN in positive x-direction at node 2. Calculate
 - (a) stiffness matrix and
 - (b) stresses. [12+8]

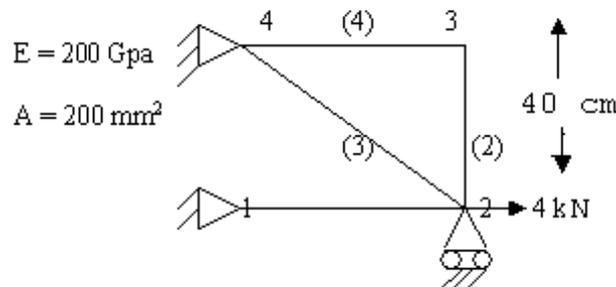


Figure 3

4. Derive the element stiffness matrix for the 2-noded beam element [20]
5. The coordinates of the nodes 1, 2 and 3 of a triangular element are (1, 1), (8, 4) and (2, 7) in mm. The displacements at the nodes are $u_1 = 1 \text{ mm}$, $u_2 = 3 \text{ mm}$, $u_3 = -2 \text{ mm}$, $v_1 = -4 \text{ mm}$, $v_2 = 2 \text{ mm}$ and $v_3 = 5 \text{ mm}$. Obtain the strain-displacement relations, matrix B and determine the strains ϵ_x , ϵ_y and γ_{xy} . [20]
6. Derive the element conductivity matrix and load vector for solving 1-D heat conduction problems, if one of the surfaces is exposed to a heat transfer coefficient of h and ambient temperature of T_∞ ? [20]
7. Consider the axial vibrations of a steel bar shown in the figure 7:
 - (a) Develop global stiffness and mass matrices,
 - (b) Determine the natural frequencies? [10+10]

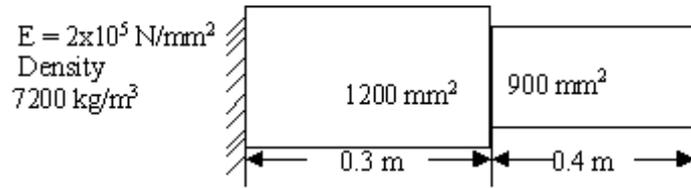


Figure 7

8. (a) How do you calculate the element stresses for 3-Dimensional body?
(b) Derive the element stiffness term and force term for four noded tetrahedral elements. [10+10]
